Basic Set Theory

- Containment. $A \subseteq B \Leftrightarrow x \in A \Rightarrow x \in B$.
- Equality. $A = B \Leftrightarrow A \subseteq B$ and $B \subseteq A$.
- Union. The *union* of A and B, written $A \cup B$, is the set of elements that belong to either A or B or both:

$$A \cup B = \{x | x \in A \text{ or } x \in B\}.$$

• Intersection. The *intersection* of A and B, written $A \cap B$, is the set of elements that belong to both A and B.

$$A \cap B = \{x | x \in A \text{ and } x \in B\}.$$

• Complement. The *complement* of A, written A^c , is the set of all elements that are not in A:

$$A^c = \{x | x \notin A\}.$$

- Properties:
 - 1. Commutativity
 - **a.** $A \cup B = B \cup A$
 - **b.** $A \cap B = B \cap A$
 - 2. Associativity
 - **a.** $A \cup (B \cup C) = (A \cup B) \cup C$
 - **b.** $A \cap (B \cap C) = (A \cap B) \cap C$
 - 3. Distributive Laws
 - **a.** $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
 - **b.** $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
 - 4. De Morgan's Laws
 - a. $(A \cup B)^c = A^c \cap B^c$
 - **b.** $(A \cap B)^c = A^c \cup B^c$